# The Use of Quadtree Range Domain Partitioning with Fast Double Moment Descriptors to Enhance FIC of Colored Image 

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#### Abstract

In this paper, an enhanced fractal image compression system (FIC) is proposed; it is based on using both symmetry prediction and blocks indexing to speed up the blocks matching process. The proposed FIC uses quad tree as variable range block partitioning mechanism. two criteria's for guiding the partitioning decision are used: The first one uses sobel-based edge magnitude, whereas the second uses the contrast of block. A new set of moment descriptors are introduced, they differ from the previously used descriptors by their ability to emphasize the weights of different parts of each block. The effectiveness of all possible combinations of double moments descriptors has been investigated. Furthermore, a fast computation mechanism is introduced to compute the moments attended to improve the overall computation cost. the results of applied tests on the system for the cases "variable and fixed range" block partitioning mechanism indicated that the variable partitioning scheme can produce better results than fixed partitioning one (that is, $4 \times 4$ block) in term of compression ratio, faster than and PSNR does not significantly decreased.


Index Terms-Fractal image compression, Iterated function system, Moments features, Quadtree.

## I. Introduction

Recently, fractal compression of digital images has attracted much attention. Fractal image compression (FIC) is based on the theory of iterated function system (IFS), and its performance relies on the presence of self-similarity degree (Mahadevaswamy, 2000). FIC process implies finding a set of transformations that produce fractal image which approximates the original image (Xi and Zhang, 2007). One of the most important characteristics of fractal image coding is its unsymmetrical property of encoding and decoding

[^0]processing. Coding time is rather long for whole domainrange matching operation, whereas the decoding algorithm is relatively simple and fast. This weak aspect makes the fractal compression method not widely used as standard compression. FIC has the advantages of fast decompression as well as very high compression ratios (CR) (Al-Hilo and George, 2008).

Many attempts have been done for speeding FIC using different speeding-up methods. An adaptive zero-mean method was proposed by (George, 2006), according to this method the average of the range block is used instead of traditional offset parameter. George method's used in combination with moment-based features (George and Al-Hilo, 2008; Al-Hilo and George, 2008) and DCT-based methods (George and Minas, 2011) as IFS transform invariants to be used as block descriptors; which in turn is utilized to classify the domain and range blocks. Furthermore, by adding the symmetry predictor that introduced in the method given in (George and Al-Hilo, 2011) that based on using first-order centralized moments; this predictor is useful to reduce the number of isometric trails from (8, that is, Rotation, reflection...etc.,) trials to (1) trail. Mahmoud, 2012 proposed the use of double moment descriptors to speed up FIC.

In the proposed method, introduced in this paper, the loaded RGB color image was transformed to YUV color space, where Y is the luminance component, and $\mathrm{U}, \mathrm{V}$ are the chromatic components. To get an effective compression, the U, V component are downsampled (Ning, 2007).Then, each component of YUV is coded individually using FIC method. An improved algorithm of FIC based on partition IFS method is applied; the improvement was in: (i) The scheme of range pool partitioning, (ii) IFS matching with low computation redundancy, and (iii) using a new set of centralized moments which are complementary and more informative.

The rest of the paper is structured as follows: Section II is dedicated to give an overview for the concepts and methods used to explain the enhance FIC system. The results of the tests applied the enhanced are discussed in Section III, and finally, the derived conclusions are listed in Section IV.

## II. Materials and methods

## A. IFS Coding for Zero-mean Blocks

IFS coding based on zero-mean blocks matching implies that the offset values of the block replacement with average brightness values. Hence, the IFS mapping equation was performed according to this change. For a range block with pixel values $\left(\mathrm{r}_{0}, \ldots, \mathrm{r}_{\mathrm{n}-1}\right)$ and a domain block with pixels $\left(\mathrm{d}_{0}, \ldots\right.$ .., $\mathrm{d}_{\mathrm{n}-1}$ ) the contractive affine approximation is (George, 2006):

$$
\begin{gather*}
\mathrm{r}_{\mathrm{i}}=\mathrm{s}\left(\mathrm{~d}_{\mathrm{i}}-\overline{\mathrm{d}}\right)+\overline{\mathrm{r}}  \tag{1}\\
\overline{\mathrm{r}}=\frac{1}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{r}_{\mathrm{i}}  \tag{2}\\
\overline{\mathrm{~d}}=\frac{1}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{~d}_{\mathrm{i}} \tag{3}
\end{gather*}
$$

Where $r_{i}$ is the optimal approximated value of the $i^{\text {th }}$ byte value of the range block; $d_{i}$ is the corresponding byte value in the best-matched domain block; $s$ is the scaling coefficient; $\overline{\mathrm{d}}, \overline{\mathrm{r}}$ are the average of domain and range block, respectively.

To determine the scale (s) value, the method of least mean square errors (depicted in equation 1) is applied to get:

$$
\begin{align*}
& \mathrm{s}= \begin{cases}\frac{\frac{1}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{~d}_{\mathrm{i}} \mathrm{r}_{\mathrm{i}}-\overline{\mathrm{rd}}}{\sigma_{\mathrm{d}}^{2}} & \text { if } \sigma_{\mathrm{d}}^{2}>0 \\
0 & \text { if } \sigma_{\mathrm{d}}^{2}=0\end{cases}  \tag{4}\\
& \mathrm{X}^{2}=\sigma_{\mathrm{r}}^{2}+\mathrm{s}\left[\mathrm{~s} \sigma_{\mathrm{d}}^{2}+2 \overline{\mathrm{~d} r} \overline{\mathrm{r}}-\frac{2}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{~d}_{\mathrm{i}} \mathrm{r}_{\mathrm{i}}\right] \tag{5}
\end{align*}
$$

Where,

$$
\begin{align*}
& \sigma_{\mathrm{d}}^{2}=\frac{1}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{~d}_{\mathrm{i}}^{2}-\overline{\mathrm{d}}^{2}  \tag{6}\\
& \sigma_{\mathrm{r}}^{2}=\frac{1}{\mathrm{n}} \sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{r}_{\mathrm{i}}^{2}-\overline{\mathrm{r}}^{2} \tag{7}
\end{align*}
$$

At each range-domain matching instance, and before determination of $\chi^{2}$ (equation 5), the scale coefficient (s) must be bounded to be in the range $\left[-\mathrm{s}_{\max }, \mathrm{s}_{\max }\right]$. Then, the scale coefficient (s) and $\bar{r}$ should be quantized using the following equations (Mahmoud, 2012):

$$
\begin{gather*}
\tilde{s}=Q_{s} I_{s}  \tag{8}\\
I_{s}=\operatorname{round}\left(\frac{\mathrm{s}}{\mathrm{Q}_{\mathrm{s}}}\right) \tag{9}
\end{gather*}
$$

$$
\begin{gather*}
\tilde{\mathrm{r}}=\mathrm{Q}_{\overline{\mathrm{r}}} \mathrm{I}_{\mathrm{r}}  \tag{10}\\
\mathrm{I}_{\mathrm{r}}=\operatorname{round}\left(\frac{\overline{\mathrm{r}}}{\mathrm{Q}_{\overline{\mathrm{r}}}}\right) \tag{11}
\end{gather*}
$$

Where

$$
\begin{gather*}
\mathrm{Q}_{\mathrm{s}}=\frac{\mathrm{s}_{\max }}{2^{\mathrm{bs}-1}-1}  \tag{12}\\
\mathrm{Q}_{\overline{\mathrm{r}}}=\frac{255}{2^{\mathrm{br}}-1} \tag{13}
\end{gather*}
$$

Where $\mathrm{s}_{\text {max }}$ is the highest permissible value of the scale coefficient (s); $Q_{s}$ and $\mathrm{Q}_{\overline{\mathrm{r}}}$ are the quantization steps of the scale and $\overline{\mathrm{r}}$ coefficients, respectively; bs is the number of scale bits; br is the number of range mean bits.

## B. Isometric Process Predictor

The eight isometric mappings are shown in Table I (George and Al-Hilo, 2009). A full search through the set of 8 isometric states of each block is prohibitive due to the large number of calculation involved. The goal is to exclude isometric states of blocks that have no chance of being selected as the best choice (George and Mahmoud, 2011).

The involved calculation for block indexing and transform prediction should be simpler than the full calculation. This would ease the burden of searching by reducing the set of possible candidates to minimal error. Hence, in this process, the speeding up of FIC is accomplished using the firstorder moments descriptor (George and Al-Hilo, 2009). The theoretical basis of this predictor of the isometric processes is described in the following sections.

## Centralized moments

For an image block $I(x, y)\{x, y \mid 0,1, \ldots, L-1\}$, its first-order centralized moments are defined as (George and Mahmoud, 2011):

$$
\begin{align*}
& M_{x}=\sum_{x=0}^{L-1} \sum_{y=0}^{L-1} I(x, y)(x-c)  \tag{14}\\
& M_{y}=\sum_{y=0}^{L-1} \sum_{x=0}^{L-1} I(x, y)(y-c) \tag{15}
\end{align*}
$$

Where $\mathrm{c}=(\mathrm{L}-1) / 2$.
Combining equations (14) and (15) with the equations listed in Table I, the relationship between the new moments values $\left(\mathrm{M}_{\mathrm{x}}, \mathrm{M}_{\mathrm{y}}^{\prime}\right)$ of a transformed block with its old moments' values $\left(M_{x}, M_{y}\right)$, before transformation, could be determined; Table II shows these relationships (George and Al-Hilo, 2009).

## Blocks classification

A method for blocks classification based on moment criteria is suggested. The classification is based on the status of its first-order moments values (that is, $\mathrm{M}_{\mathrm{x}}$ and $\mathrm{M}_{\mathrm{y}}$ ). The following three status criteria have been used where:

- Condition-1: Is $\left|M_{x}\right| \geq\left|M_{y}\right|$ or not?
- Condition-2: Is $\mathrm{M}_{\mathrm{x}} \geq 0$ or not?
- Condition-3: Is $\mathrm{M}_{\mathrm{y}} \geq 0$ or not?

The use of these three Boolean criteria leads to eight block classes as illustrated in Table III (George and Al-Hilo, 2001).

At each range-domain matching instance, the indices of both domain and range blocks are passed through the predictor, as shown in Table IV. Then, the predictor outputs the index of the required isometric transform to get the best possible match between the domain and range blocks (George and Mahmoud, 2011).

## C. Moment's Ratio and Index

Moment's ratio can be calculated using the following equation by (Mahmoud, 2012):

$$
\text { Ratio }_{M}= \begin{cases}\left|\frac{M_{y}}{M_{x}}\right| \times N m & \text { if } M_{x} \geq M_{y}  \tag{16}\\ \left|\frac{M_{x}}{M_{y}}\right| \times N m & \text { if } M_{y} \geq M_{x}\end{cases}
$$

Where $M_{x}$ and $M_{y}$ are the moments around $x$ and $y$ coordinates, respectively. Nm is the maximum moment ratio value. Al-Hilo and George, 2008 concluded that "If the two blocks (range and domain) nearly satisfy the conductive affine transform, then their moment ratio factor Ratio $_{\text {Mr }}$

TABLE I
Isometric Transformation (George and al-hilo, 2009).

| ID | Operation | Equation | Results |
| :--- | :--- | :--- | :--- |
| 0 | Identity | $x^{\prime}=x \cos (0)-y \sin (0)$ | $x^{\prime}=x$ |
|  |  | $y^{\prime}=-x \sin (0)+y \cos (0)$ | $y^{\prime}=y$ |
| 1 | Rotation $(+90)$ | $x^{\prime}=x \cos (90)-y \sin (90)$ | $x^{\prime}=y$ |
|  |  | $y^{\prime}=-x \sin (90)+y \cos (90)$ | $y^{\prime}=-x$ |
| 2 | Rotation $(+180)$ | $x^{\prime}=x \cos (180)-y \sin (180)$ | $x^{\prime}=-x$ |
|  |  | $y^{\prime}=-x \sin (180)+y \cos (180)$ | $y^{\prime}=-y$ |
| 3 | Rotation (+270) | $x^{\prime}=x \cos (270)-y \sin (270)$ | $x^{\prime}=-y$ |
|  |  | $y^{\prime}=-x \sin (270)+y \cos (270)$ | $y^{\prime}=x$ |
| 4 | Reflection around X-axis | $x^{\prime}=-x \cos (0)-y \sin (0)$ | $x^{\prime}=-x$ |
| 5 | Reflection around | $y^{\prime}=-x \sin (0)+y \cos (0)$ | $y^{\prime}=y$ |
|  | X-axis+Rotation(+90) | $x^{\prime}=-x \cos (90)-y \sin (90)$ | $x^{\prime}=-x \sin (90)+y \cos (90)$ |
| 6 | Reflection around | $y^{\prime}=-x$ |  |
|  | X-axis+Rotation(+180) | $y^{\prime}=-x \cos (180)-y \sin (180)$ | $x^{\prime}=-x \sin (180)+y \cos (180)$ |
| 7 | Reflection around | $y^{\prime}=-y$ |  |
|  | X-axis+Rotation(+270) | $x^{\prime}=-x \cos (270)-y \sin (270)$ | $x^{\prime}=y$ |

TABLE II
The Relationship between Moments before and after Applying the Isometric Transformation (George and al-hilo, 2009)

| ID | Operation | Relationship |
| :---: | :---: | :---: |
| 0 | Identity | $\mathrm{M}_{\mathrm{x}}^{\prime}=\mathrm{M}_{\mathrm{x}}, \mathrm{M}_{\mathrm{y}}^{\prime}=\mathrm{M}_{\mathrm{y}}$ |
| 1 | Rotation (+90) | $M_{x}^{\prime}=M_{y}, M_{y}^{\prime}=-M_{x}$ |
| 2 | Rotation (+180) | $\mathrm{M}^{\prime}{ }_{\mathrm{x}}=-\mathrm{M}_{\mathrm{x}}, \mathrm{M}^{\prime}{ }_{\mathrm{y}}=-\mathrm{M}_{\mathrm{y}}$ |
| 3 | Rotation (+270) | $M^{\prime}{ }_{x}=-M_{y}, M^{\prime}{ }^{\prime}=M_{x}$ |
| 4 | Reflection at X -axis | $M^{\prime}{ }_{x}=-M_{x}, M^{\prime}{ }_{y}=M_{y}$ |
| 5 | Reflection around X-axis + rotation ( $+90^{\circ}$ ) | $M^{\prime}{ }_{x}^{\prime}=-M_{y}, M_{y}^{\prime}=-M_{x}$ |
| 6 | Reflection around X-axis+rotation ( $+180^{\circ}$ ) | $M^{\prime}{ }_{x}^{\prime}=M_{x}, M_{y}^{\prime}=-M_{y}$ |
| 7 | Reflection around X-axis+rotation ( $+270^{\circ}$ ) | $\mathrm{M}_{\mathrm{x}}^{\prime}=\mathrm{M}_{\mathrm{y}}, \mathrm{M}_{\mathrm{y}}^{\prime}=\mathrm{M}_{\mathrm{x}}$ |

and Ratio $_{M d}$ ) should have similar values, this does not mean that any two blocks have similar ( Ratio $_{M}$ ) factor should necessarily satisfy the affine transform."

The value of combined moment ratio index is computed as the linear combination of two descriptors ( Ratio $_{M 1}$ ) and ( Ratio $_{\text {M }}$ ) using the following equation (Mahmoud, 2012).

$$
\begin{equation*}
I_{M}=\left[\text { Ratio }_{M 1} \times(N m+1)+\text { Ratio }_{M 2}\right] \tag{17}
\end{equation*}
$$

The index $\left(I_{M}\right)$ is used to classify the domain and range blocks (that is, each class includes blocks having the same index). This factor is used to improve (that is, speeding up) the range-domain search task by only the domain blocks whose $I_{M}$ values are similar (or near) to that of tested range block are IFS-matched.

## D. The Proposed FIC

The aims of the enhanced FIC are:

- A new set of moment descriptors are introduced, they differ from the previously used ones by their excellent emphasis to reflect the moments' weight of certain part of the block. In this article, the effectiveness of all possible combinations of double moment descriptors had been investigated.
- Quadtree (QT) is used to enhance IFS performance. It is used as variable range blocks partitioning scheme instead of fixed block partitioning scheme. The criteria guiding the decomposition

TABLE III
The Truth Table for Eight Block Classes (Mahmoud, 2012)

| Block class ID | Boolean criteria |  |  |
| :--- | :--- | :--- | :--- |
|  | $\left\|\mathrm{M}_{\mathrm{x}}\right\| \geq\left\|\mathrm{M}_{\mathrm{y}}\right\|$ | $\mathrm{M}_{\mathrm{x}} \geq 0$ | $\mathrm{M}_{\mathrm{y}} \geq 0$ |
| 0 | T | T | T |
| 1 | T | T | F |
| 2 | T | F | T |
| 3 | T | F | F |
| 4 | F | T | T |
| 5 | F | T | F |
| 6 | F | F | T |
| 7 | F | F | F |

0-Identity, 1 - Rotation (+90), 2 - Rotation (+180), 3 - Rotation (+270),
4 -Reflection, 5 -Reflection + rotation ( +90 ), $6-$ Reflection + Rotation $(+180)$,
7 - Reflection + Rotation (+270).

TABLE IV
The Required Isometric Operation to Convert the Block State (George and Mahmoud, 2011)

| Range <br> blocks ID | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 0 | 6 | 4 | 2 | 7 | 3 | 1 | 5 |
| 0 | 6 | 0 | 2 | 4 | 1 | 5 | 7 | 3 |
| 1 | 4 | 2 | 0 | 6 | 3 | 7 | 5 | 1 |
| 2 | 2 | 4 | 6 | 0 | 5 | 1 | 3 | 7 |
| 3 | 7 | 3 | 1 | 5 | 0 | 6 | 4 | 2 |
| 4 | 1 | 5 | 7 | 3 | 6 | 0 | 2 | 4 |
| 5 | 3 | 7 | 5 | 1 | 4 | 2 | 0 | 6 |
| 6 | 5 | 1 | 3 | 7 | 2 | 4 | 6 | 0 |
| 7 |  |  |  |  |  |  |  |  |

process is the information richness of the region; it was used to decide the initial partitioning of the range blocks.

- FIC algorithm is reconfigured including the moment equations to remove any redundancy in the computation.

In the following subsection, the proposed enhanced FIC is explained in more details.

The proposed moments and the speeding up mechanism
A new set of weights is introduced and adopted to produce the new sets of moments, they are as follows:

$$
\begin{align*}
& \mathrm{W}_{1}(\mathrm{i})=\left\{\begin{array}{cc}
\frac{2}{\mathrm{~L}}\left(\mathrm{i}-\frac{\mathrm{L}}{2}\right) & \text { for } \mathrm{i}=\left[0, \frac{\mathrm{~L}}{2}\right) \\
-\mathrm{W}_{1}(\mathrm{~L}-1-\mathrm{i}) & \text { for } \mathrm{i}=\left[\frac{\mathrm{L}}{2}-1, \mathrm{~L}\right)
\end{array}\right.  \tag{18-a}\\
& \mathrm{W}_{1}^{\text {int }}(\mathrm{i})=\mathrm{W}_{1}(\mathrm{i}) \times 100 \text { for } \mathrm{i}=[0, \mathrm{~L})  \tag{18-b}\\
& \mathrm{W}_{2}(\mathrm{i})=\left\{\begin{array}{cc}
\frac{2}{\mathrm{~L}}\left(\mathrm{i}-\frac{1}{2}\right) & \text { for } \mathrm{i}=\left[0, \frac{\mathrm{~L}}{2}\right) \\
-\mathrm{W}_{2}(\mathrm{~L}-1-\mathrm{i}) & \text { for } \mathrm{i}=\left[\frac{\mathrm{L}}{2}-1, \mathrm{~L}\right)
\end{array}\right.  \tag{19-a}\\
& W_{2}^{\text {int }}(i)=W_{2}(i) \times 100 \quad \text { for } i=[0, L)  \tag{19-b}\\
& W_{3}(i)=\left\{\begin{array}{cc}
\sin \left(\frac{\Pi i}{L-1}\right) & \text { for } i=\left[0, \frac{\mathrm{~L}}{2}\right) \\
-\mathrm{W}_{3}(\mathrm{~L}-1-\mathrm{i}) & \text { for } \mathrm{i}=\left[\frac{\mathrm{L}}{2}-1, \mathrm{~L}\right)
\end{array}\right.  \tag{20-a}\\
& W_{3}^{\text {int }}(i)=W 3(i) \times 100 \quad \text { for } i=[0, L) \tag{20-b}
\end{align*}
$$

Fig. 1 presents the proposed three weight functions that assigned to each row or column within the block, when its length is equal to 8 .

The new sets of moments around $x$-axis and around $y$-axis that using the weights functions given in equations (18-20) are defined as:


Fig. 1. The proposed weights.

$$
\begin{align*}
& \mathrm{Mx}_{1}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1 \mathrm{c}+\mathrm{L}-1} \sum_{\mathrm{c}=\mathrm{y}} \mathrm{f}(\mathrm{r}, \mathrm{c}) \mathrm{W}_{1}^{\text {int }}(\mathrm{r}-\mathrm{x})  \tag{21-a}\\
& \mathrm{My}_{1}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{c}=\mathrm{y}}^{\mathrm{c}+\mathrm{L}-1 \mathrm{r}+\mathrm{L}-1} \sum_{\mathrm{r}=\mathrm{x}} \mathrm{f}(\mathrm{r}, \mathrm{c}) \mathrm{W}_{1}^{\text {int }}(\mathrm{c}-\mathrm{y})  \tag{21-b}\\
& \mathrm{Mx}_{2}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1 \mathrm{c}+\mathrm{L}-1} \sum_{\mathrm{c}=\mathrm{y}} \mathrm{f}(\mathrm{r}, \mathrm{c}) \mathrm{W}_{2}^{\text {int }}(\mathrm{r}-\mathrm{x})  \tag{22-a}\\
& M y_{2}(x, y)=\sum_{c=y}^{c+L-1} \sum_{r=x}^{r+L-1} f(r, c) W_{2}^{\text {int }}(c-y)  \tag{22-b}\\
& \mathrm{Mx}_{3}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1 \mathrm{c}+\mathrm{L}-1} \sum_{\mathrm{c}=\mathrm{y}} \mathrm{f}(\mathrm{r}, \mathrm{c}) \mathrm{W}_{3}^{\mathrm{int}}(\mathrm{r}-\mathrm{x})  \tag{23-a}\\
& \mathrm{My}_{3}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{c}=\mathrm{y}}^{\mathrm{c}+\mathrm{L}-1 \mathrm{r}+\mathrm{L}-1} \sum_{\mathrm{r}=\mathrm{x}} \mathrm{f}(\mathrm{r}, \mathrm{c}) \mathrm{W}_{3}^{\text {int }}(\mathrm{c}-\mathrm{y}) \tag{23-b}
\end{align*}
$$

Where $L$ represents the length of the block; $(x, y)$ are coordinates of the block relative to left-top corner; $F()$ is the 2 D image array; $W^{\text {nt }}$ represents the integer index of the weights; $M x$ represents the low-order moments relative to x-axis; My represents the low-order moments relative to $y$-axis.

So, for each block, of the overlapped blocks listed in the domain pool, the moments (given by equations 21-23) have been computed. For fast computations of the moment descriptor equations the following scenario adopted to avoid the redundant summation occurs within each one by creating two 2D arrays, named "SumX" and "SumY," such that:

$$
\begin{gather*}
\operatorname{SumX}(x, 0)=\sum_{y=0}^{\mathrm{L}-1} f(x, y)  \tag{24}\\
\operatorname{Sum} X(x, y)=\operatorname{SumX}(x, y-1)-f(x, y-1)+f(x, y+L-1) \\
\operatorname{SumY}(0, y)=\sum_{x=0}^{\mathrm{L}-1} f(x, y)  \tag{25}\\
\operatorname{SumY}(x, y)= \\
=\operatorname{Sumy}(x-1, y)-Y B(x-1, y)  \tag{27}\\
+ \\
\operatorname{YB}(x+L-1, y)
\end{gather*}
$$

Fig. 2 shows simple example of how the value of $\operatorname{Sum} X$ $(0,0)$ and $\operatorname{Sum} X(0,1)$ had been computed for row sample when block length $(L)$ equal to 8 .

Now, the created arrays $\operatorname{Sum} X$ and $\operatorname{Sum} Y$ can be used in (21-23) to become as:

$$
\begin{equation*}
\mathrm{Mx}_{1}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1} \operatorname{SumX}(\mathrm{r}, \mathrm{y}) \times \mathrm{W}_{1}^{\text {int }}(\mathrm{r}-\mathrm{x}) \tag{28a}
\end{equation*}
$$



Fig. 2. Shows simple example of how the value of $\operatorname{Sum} X(0,0)$ and $\operatorname{SumX}(0,1)$ had been computed for row sample when block length (L) equal to 8 .

$$
\begin{align*}
& \mathrm{My}_{1}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{c}=\mathrm{y}}^{\mathrm{y}+\mathrm{L}-1} \operatorname{Sum} \mathrm{Y}(\mathrm{x}, \mathrm{c}) \times \mathrm{W}_{1}^{\text {int }}(\mathrm{c}-\mathrm{y})  \tag{28b}\\
& \mathrm{Mx}_{2}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1} \operatorname{Sum} \mathrm{X}(\mathrm{r}, \mathrm{y}) \times \mathrm{W}_{2}^{\text {int }}(\mathrm{r}-\mathrm{x})  \tag{29a}\\
& \mathrm{My}_{2}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{c}=\mathrm{y}}^{\mathrm{y}+\mathrm{L}-1} \operatorname{SumY}(\mathrm{x}, \mathrm{c}) \times \mathrm{W}_{2}^{\text {int }}(\mathrm{c}-\mathrm{y})  \tag{29b}\\
& \mathrm{Mx}_{3}(\mathrm{x}, \mathrm{y})=\sum_{\mathrm{r}=\mathrm{x}}^{\mathrm{r}+\mathrm{L}-1} \operatorname{SumX}(\mathrm{r}, \mathrm{y}) \times \mathrm{W}_{3}^{\text {int }}(\mathrm{r}-\mathrm{x})  \tag{30a}\\
& \mathrm{My}_{3}(\mathrm{x}, \mathrm{y})=\sum_{c=y}^{y+L-1} \operatorname{SumY}(\mathrm{x}, \mathrm{c}) \times \mathrm{W}_{3}^{\text {int }}(\mathrm{c}-\mathrm{y}) \tag{30b}
\end{align*}
$$

As mentioned above, the effectiveness of using the three possible pairs of moments combinations, to compute the blocks descriptors that used for indexing to speeding up the range-domain search task, \{that is, $\left(M_{p}, M_{2}\right),\left(M_{p}, M_{3}\right)$, and $\left.\left(M_{2}, M_{3}\right)\right\}$ have been investigated.

## The proposed range pool partitioning scheme

The proposed partitioning scheme that applied to generate the range pool blocks is the quadtree; it partitions the range array into nonoverlapped variable length blocks. Two criteria have been used to guide the decomposition process; the first is based on the edge detection using Sobel filter (see equations 31a and b ) and the second based on the contrast (see equation 32). The permissible block length (PBL) is 8 and 4 :

$$
\begin{gather*}
\mathrm{G}_{\mathrm{x}}=\left[\begin{array}{ccc}
-1 & -2 & -1 \\
0 & 0 & 0 \\
1 & 2 & 1
\end{array}\right]  \tag{31a}\\
\mathrm{G}_{\mathrm{y}}=\left[\begin{array}{ccc}
-1 & 0 & 1 \\
-2 & 0 & 2 \\
-1 & 0 & 1
\end{array}\right] \tag{31b}
\end{gather*}
$$

For the block addressed as $\left[\begin{array}{cc}(x, y) & (x, y+1) \\ (x+1, y) & (x+1, y+1)\end{array}\right]$ the maximum variance around the pixel $(x, y)$ is computed as

$$
\operatorname{Max}_{\mathrm{var}}=\operatorname{Max}\left(\begin{array}{c}
|\operatorname{pixel}(\mathrm{x}, \mathrm{y})-\operatorname{pixel}(\mathrm{x}, \mathrm{y}+1)|  \tag{32}\\
|\operatorname{pixel}(\mathrm{x}, \mathrm{y})-\operatorname{pixel}(\mathrm{x}+1, \mathrm{y})| \\
|\operatorname{pixel}(\mathrm{x}, \mathrm{y})-\operatorname{pixel}(\mathrm{x}+1, \mathrm{y}+1)|
\end{array}\right)
$$

The regions threshold determined according to the following relation:

$$
\operatorname{Thr}_{\mathrm{Q}}=\left\{\begin{array}{cc}
\mathrm{val}_{\mathrm{var}} & \text { if use Max }  \tag{33}\\
\operatorname{val}_{\text {Sobel }} & \text { if use } \mathrm{Max}_{\text {Sobel }}
\end{array}\right.
$$

Where val $_{\text {var }} \in\{10,12,14 ., 30\}$, while val $_{\text {sobel }} \in\{30,35,40, \ldots, 90\}$. These threshold values were selected after comprehensive tests.

The partitioning process started by partitioning the range array into nonoverlapped block of size equal to (8). For each block, one of the following steps is done:

- If Sobel filter used as a decision to partition the current block, then the highest value between $\mathrm{G}_{\mathrm{x}}$ or $\mathrm{G}_{\mathrm{y}}$ over the tested block determined,
- If the maximum variance is used as a decision to partition this block, then the maximum variance over all pixels belong to the block are determined.
If the determined value exceeds the predetermined $T h r_{Q}$, then split the block into four quadrants.

Fig. 3a shows the well-known Baboon image after applying the proposed partitioning scheme that used Sobel as partitioning decision (where the threshold value $\mathrm{val}_{\text {sobol }}$ is set 40). While Fig. 3b shows the well known Lenna image after applying the proposed partitioning scheme that based on maximum variance as partitioning decision (where the threshold value val variance is set to 22).

## Enhanced FIC encoding process

The introduced enhanced encoding algorithm of the range blocks are summarized by the following steps:
a) Load BMP image and put it in (R,G,B) array (three 2D arrays)
b) Convert (R,G,B) array to (Y,U,V) array
c) Downsample the components $U$ and $V$
d) Determine the moment combinations used
e) For each color component (that is, the original Y, and the downsampled $[\mathrm{U}, \mathrm{V}]$ ) do the followings:

1. Construct the domain and range pools. This process is done by partitioning the range array into nonoverlapping variable blocks (using the above-mentioned quadtree method with one of the partitioning decision stated in section 2.4.2) to generate the range $\left(r_{0}, . . r_{n-1}\right)$ blocks.
2. Set the PBL to 8 .
3. The downsampled range array (that is, the domain array) is partitioned into overlapped fixed blocks of size equal to PBL to generate the domain $\left(\mathrm{d}_{0}, . . \mathrm{d}_{\mathrm{m}-1}\right)$ blocks.
4. For each domain block listed in domain pool do the following:
i. Determine the average $(\overline{\mathrm{d}})$ using equation 3 .
ii. Determine the $\left(n \sigma_{d}^{2}\right)$ as:

$$
\begin{equation*}
\mathrm{n} \sigma_{\mathrm{d}}^{2}=\sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{~d}_{\mathrm{i}}^{2}-\mathrm{n} \overline{\mathrm{~d}}^{2} \tag{34}
\end{equation*}
$$

iii. Determine the moments using equations (28-30) that corresponding to the selected moments.
iv. Determine the moment ratio for each moment using equation 16.
v. Determine the moment index value using equation 17.
vi. Determine the block isometric index (Sym_indxd) that based on moment order one (that is, equations $(14,15)$ and Table III).
5. Store the position coordinates $\left(x_{d}, y_{d}\right)$ of the domain blocks and the calculated moment index in temporary array (L) of record.
6. Sort the array of record (L) in ascending order according to their moment index.
7. Establish a set $(\mathrm{P})$ of pointers referring to the start and end of records holding the same index value.
8. For each range, block of size equal to PBL do the following: i. Calculate the average $(\overline{\mathrm{r}})$ using equation 2.
ii. Determine the $\left(\mathrm{n} \sigma_{\mathrm{d}}^{2}\right)$ as:

$$
\begin{equation*}
\mathrm{n} \sigma_{\mathrm{r}}^{2}=\sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{r}_{\mathrm{i}}^{2}-\mathrm{n} \overline{\mathrm{r}}^{2} \tag{35}
\end{equation*}
$$

iii. Determine the moments using equations (28-30) that corresponding to the selected moments.
iv. Determine the moment ratio for each moment using equation 16.
v. Determine the moment index value using equation 17.
vi. Determine the block isometric index (Sym_indxr) that based on moment order one (that is, equations $(14,15)$ and Table III).
9. With help of pointers set (p) and the temporary list of records (L); match only the domain blocks whose moment index values equal to the range index value.
10. The parameters Sym_indxr and sym_indxd are passed through the isometric predictor; the predictor will output


Fig. 3. (a and b) The proposed variable partitioning scheme applied on some test images.
the index of the required isometric transform (using Table IV). Then, apply the assigned transform on the tested range block.
11. The proposed enhanced steps for fast computation of $s$ and $\chi^{2}$ is applied using the following equations:

$$
\begin{gather*}
\phi=\sum_{\mathrm{i}=0}^{\mathrm{n}-1} \mathrm{r}_{\mathrm{i}} \mathrm{~d}_{\mathrm{i}}-\mathrm{n} \overline{\mathrm{r}} \overline{\mathrm{~d}}  \tag{36}\\
\mathrm{~s}=\frac{\phi}{\mathrm{n} \sigma_{\mathrm{d}}^{2}}  \tag{37}\\
\chi^{2}=\mathrm{n} \sigma_{\mathrm{r}}^{2}+\mathrm{s}^{2} \mathrm{n} \sigma_{\mathrm{d}}^{2}-2 \mathrm{~s} \phi \tag{38}
\end{gather*}
$$

Then, calculate the scale coefficient (s) and $\left(\chi^{2}\right)$ of first class of the domain blocks with range block and apply the following steps:
i. Compare the result $\left(\chi^{2}\right)$ of each matching instance with the $\left(\chi_{\text {min }}^{2}\right)$ that registered during the previous matching instances. If the compared ( is smaller than $\left(\chi^{2}{ }_{\text {min }}\right)$, then put its value in $\left(\chi_{\text {min }}^{2}\right)$ and register (s) beside to the average mean value of range block and the position and symmetry state (sym) of the domain block.
ii. If the $\left(\chi_{\text {min }}^{2}\right)<$ minimum blockerror, then the search across the domain blocks is stopped and the registered domain blocks are considered as the best match, output the set values (position, symmetry state, $s, \bar{r}$ ) and go to 4 .
iii. Otherwise, start test the domain blocks that closest higher class.
12. Divide PBL by 2, if the result equal to 2 then, stop the search, else go to 3 .

## III. Test results

The proposed system was implemented using Embarcadero RAD Studio 2010 Visual Pascal Programming Language programming language. The tests were conducted under the environment: Windows-8 operating system, laptop computer - Lenovo (processor: Intel (R) Core(TM) i5-3337U, CPU 1.8 GHz , and 4GB RAM). The tests were applied on the well-known Lena and Baboon image samples (whose specifications are: Size $=$ $256 \times 256$ pixel, color depth $=24$ bit). To assess the difference between the reconstructed image and the original images, the error measures (that is, mean square error MSE and peak signal

TABLE V
The Values of the Control Parameters

| Parameter | Range or value |
| :--- | :---: |
| $S_{\text {max }}$ | 3 |
| bs | 6 |
| br | 8 |
| Minimum Block Error $^{\text {Val }_{\text {variance }}}$ | 1 |
| Val $_{\text {Sobel }}$ | $\{10,12,14, ., 30\}$ |
| Nm | $\{30,35,40, ., 90\}$ |

to noise ratio PSNR measured in dB ) were used. Beside these fidelity measures, some complementary measures were used to describe the performance of the system; both the CR and bit rate parameters (BR) were used to describe the compression gain.

Table V lists the considered control parameters (including their names and default values); these values were selected after making comprehensive tests.

Table VI lists the notations with their descriptions that are used in the figures and tables presented in this section.

## A. Moment Combination Test

In this set of tests, the effects of using the different combinations of proposed moments are illustrated, when the blocks have been partitioned fixedly to $(4 \times 4)$. (that is, PFIC4) as listed in Tables VII and VIII.

The parameters values listed the shaded rows in Tables VII and VIII were adopted to study the effect of the proposed moment combinations' on (CR, ET, and PSNR) with the test samples explained in Fig. 4.

From the listed results, it is obvious that T 1 is the best-balanced combination. Since if the combinations sorted

TABLE VI
The Notations Used in the Test Results

| Notation | Description |
| :--- | :--- |
| T0 | The moment index ratio computed from the combination of M1 <br> and M2 |
| T1 | The moment index ratio computed from the combination of M1 <br> and M3 |
| T2 | The moment index ratio computed from the combination of M2 <br> and M3 |
| PFIC4 | The proposed FIC applied with fixed block partitioning of size <br> equal to 4 |
| PFIC8 | The proposed FIC applied with fixed block partitioning of size <br> equal to 4 |
| PFICS | The proposed FIC applied with quadtree partitioning scheme that <br> used Sobel as partitioning decision <br> The proposed FIC applied with quadtree partitioning scheme that <br> used variance as partitioning decision |
| PFICV |  |

TABLE VII
Test Results of Pfic4 When Applied on Lena Image

| Moments <br> combination | Nm | CR | MSE | PSNR | BR | ET (s) |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| T0 | 25 | 8.021 | 94.062 | 28.397 | 2.992 | 0.313 |
|  | 30 | 8.027 | 8.021 | 28.262 | 2.990 | 0.235 |
|  | 35 | 7.963 | 94.106 | 28.395 | 3.014 | 0.252 |
|  | 40 | 7.964 | 97.966 | 28.220 | 3.013 | 0.244 |
|  | 45 | 7.967 | 100.526 | 28.108 | 3.012 | 0.231 |
|  | 50 | 7.980 | 106.446 | 27.860 | 3.008 | 0.235 |
| T1 | 25 | 8.027 | 95.281 | 28.341 | 2.990 | 0.250 |
|  | 30 | 8.014 | 100.351 | 28.116 | 2.995 | 0.192 |
|  | 35 | 7.964 | 95.647 | 28.324 | 3.014 | 0.212 |
|  | 40 | 7.965 | 99.035 | 28.173 | 3.013 | 0.218 |
|  | 45 | 7.974 | 102.785 | 28.012 | 3.010 | 0.208 |
|  | 50 | 7.977 | 107.596 | 27.813 | 3.009 | 0.209 |
| T2 | 25 | 8.026 | 90.288 | 28.575 | 2.990 | 0.324 |
|  | 30 | 8.032 | 96.783 | 28.273 | 2.988 | 0.247 |
|  | 35 | 7.964 | 92.078 | 28.489 | 3.013 | 0.268 |
|  | 40 | 7.969 | 98.046 | 28.217 | 3.012 | 0.259 |
|  | 45 | 7.981 | 100.263 | 28.119 | 3.007 | 0.256 |
|  | 50 | 7.983 | 103.335 | 27.988 | 3.006 | 0.254 |

according to the maximum CR , the result is (T2, T0, and then T 1 ), and the lowest attained ET result is (T1, T0, and then T 2 ). It is difficult to arrange ( $\mathrm{T} 0, \mathrm{~T} 1$, and T 2 ) according to the PSNR because there is no significant difference with test images.

## B. PFIC4 and PFIC8 Versus PFICS Test

In this section, the proposed FIC was applied with quadtree partitioning scheme that using Sobel filter as partitioning decision (PFICS). The tests were conducted to investigate the effect of the proposed quadtree partitioning with moment combination versus fixed block partitioning (PFICL); the value of $L$ is set equal to (4 and 8) with same moment combinations listed in Table IX. Fig. 5 illustrates

TABLE VIII
Test Results of Pfic4 When Applied on Baboon Image

| Moments <br> combination | Nm | CR | MSE | PSNR | BR | ET <br> (s) |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| T0 | 25 | 8.017 | 489.506 | 21.233 | 2.994 | 0.221 |
|  | 30 | 7.984 | 499.533 | 21.145 | 3.006 | 0.199 |
|  | 35 | 7.948 | 516.252 | 21.002 | 3.020 | 0.183 |
|  | 40 | 7.952 | 519.355 | 20.976 | 3.018 | 0.194 |
|  | 45 | 7.952 | 529.911 | 20.889 | 3.018 | 0.183 |
|  | 50 | 7.952 | 549.678 | 20.730 | 3.018 | 0.182 |
| T1 | 25 | 8.016 | 493.163 | 21.201 | 2.994 | 0.204 |
|  | 30 | 7.985 | 503.922 | 21.107 | 3.006 | 0.187 |
|  | 35 | 7.947 | 518.631 | 20.982 | 3.020 | 0.176 |
|  | 40 | 7.950 | 521.902 | 20.955 | 3.019 | 0.188 |
|  | 45 | 7.952 | 535.173 | 20.846 | 3.018 | 0.176 |
| T2 | 50 | 7.951 | 549.090 | 20.734 | 3.019 | 0.179 |
|  | 25 | 8.025 | 484.939 | 21.274 | 2.991 | 0.259 |
|  | 30 | 7.990 | 497.737 | 21.161 | 3.004 | 0.228 |
|  | 35 | 7.952 | 506.847 | 21.082 | 3.018 | 0.215 |
|  | 40 | 7.951 | 513.062 | 21.029 | 3.018 | 0.219 |
|  | 45 | 7.951 | 523.084 | 20.945 | 3.019 | 0.211 |
|  | 50 | 7.952 | 539.883 | 20.808 | 3.018 | 0.207 |

TABLE IX
Test Results for Pfics and Pfics When the Moment Combination is t1, nm=50, and the Tested Sample is Baboon Image

| A. PFICS results |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Val $_{\text {Sobel }}$ | CR | MSE | PSNR | BR | ET (sec) |
| 30 | 8.160 | 568.479 | 20.584 | 2.941 | 0.116 |
| 35 | 8.401 | 571.162 | 20.563 | 2.857 | 0.110 |
| 40 | 8.603 | 573.228 | 20.548 | 2.790 | 0.105 |
| 45 | 8.774 | 574.969 | 20.534 | 2.735 | 0.105 |
| 50 | 9.033 | 578.903 | 20.505 | 2.657 | 0.101 |
| 55 | 9.247 | 580.188 | 20.495 | 2.595 | 0.098 |
| 60 | 9.432 | 584.204 | 20.465 | 2.544 | 0.096 |
| 65 | 9.608 | 585.074 | 20.459 | 2.498 | 0.095 |
| 70 | 9.752 | 587.470 | 20.441 | 2.461 | 0.095 |
| 75 | 9.930 | 590.511 | 20.419 | 2.417 | 0.096 |
| 80 | 10.060 | 593.388 | 20.397 | 2.386 | 0.093 |
| 85 | 10.292 | 599.283 | 20.355 | 2.332 | 0.093 |
| 90 | 10.477 | 604.115 | 20.320 | 2.291 | 0.090 |
| B. PFIC4 and 8 results |  |  |  |  |  |
| L | CR | MSE | PSNR | BR | ET (s) |
| 4 | 7.951 | 549.090 | 20.734 | 3.019 | 0.179 |
| 8 | 31.829 | 844.843 | 18.863 | 0.754 | 0.053 |



Fig. 4. (a-c) The effect of moment type with test images.

c
Fig. 5. (a-c) The effect $\mathrm{Val}_{\text {Sobel }}$.


Fig. 6. (a-c) The effect of proposed variable partitioning scheme using Sobel with fixed one.
the effect of $\mathrm{Val}_{\text {sobel }}$ on CR, ET, and PSNR when PFICS had been applied.

The parameters values in the listed shaded rows of Table IX have been used to compare the performance of variable and fixed partitioning scheme; the attained results are presented in Fig. 6.

## C. PFIC4 and PFIC8 Versus PFICV Test

In this section, the proposed FIC was applied with quadtree partitioning scheme that using max variance as

partitioning decision (PFICV). The tests were conducted to investigate the effect of the proposed quadtree partitioning with moment combination versus (PFICL) fixed block partitioning; the value of $L$ is set to (4 and 8) with the same moment combinations listed in Table X. Fig. 7 illustrates the effect of Val
$\mathrm{al}_{\text {varianc }}$ on CR, ET and PSNR when PFICV was applied.

The parametric values of the shaded rows listed in Table X have been used to extract the results shown in Fig. 8 to compare the performance of variable and fixed partitioning scheme.


Fig. 7. (a-c) The effect $\mathrm{Val}_{\text {variance }}$.


Fig. 8. (a-c) The effect of the proposed variable partitioning scheme using max variance with fixed one.

Table X.
Pfics test when moment combination is t 1 , $\mathrm{NM}=50$ and the test image is LENA

| A. PFICV results |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Val $_{\text {variance }}$ | CR | MSE | PSNR | BR | ET (sec) |
| 10 | 9.321 | 113.734 | 27.572 | 2.575 | 0.139 |
| 12 | 10.108 | 120.344 | 27.327 | 2.374 | 0.125 |
| 14 | 10.803 | 122.395 | 27.253 | 2.222 | 0.119 |
| 16 | 11.377 | 123.949 | 27.198 | 2.110 | 0.112 |
| 18 | 11.919 | 125.725 | 27.137 | 2.014 | 0.110 |
| 20 | 12.497 | 128.012 | 27.058 | 1.921 | 0.103 |
| 22 | 13.095 | 129.634 | 27.004 | 1.833 | 0.102 |
| 24 | 13.705 | 131.865 | 26.930 | 1.751 | 0.099 |
| 26 | 14.280 | 133.470 | 26.877 | 1.681 | 0.094 |
| 28 | 14.886 | 138.039 | 26.731 | 1.612 | 0.094 |
| 30 | 15.184 | 138.930 | 26.703 | 1.581 | 0.092 |
| B. PFIC4 and 8 results |  |  |  |  |  |
| L | CR | MSE | PSNR | BR | ET (s) |
| 4 | 7.977 | 107.596 | 27.813 | 3.009 | 0.209 |
| 8 | 32.115 | 229.912 | 24.515 | 0.747 | 0.064 |

## IV. Conclusions

From the results of tests conducted on the proposed system, the following remarks were stimulated:

1. The quadtree partitioning that guided by Sobel or variance can be considered as useful partitioning mechanism.
2. The proposed FIC that uses double moment with variable partitioning schemes produces better results than that of fixed partitioning as shown in Figs. 6 and 8.
3. The proposed moments are suitable to perform double block description which in turn can significantly speed up the IFS encoding process.
4. For future work:
a. A new criteria could be adopted for quadtree partitioning.
b. Investigate the combination of triple moments.

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